

## 1 Coordinate Systems and Vector Math

$$\begin{aligned}
 (x, y, z) &\Leftrightarrow (r, \theta, z) & x = r \cos \theta & r = \sqrt{x^2 + y^2} \\
 && y = r \sin \theta & \theta = \tan^{-1} \frac{y}{x} \\
 \hat{e}_r &= \cos \theta \hat{e}_x + \sin \theta \hat{e}_y & \hat{e}_\theta &= -\sin \theta \hat{e}_x + \cos \theta \hat{e}_y \\
 && x = \rho \sin \theta \cos \phi & \rho = \sqrt{x^2 + y^2 + z^2} \\
 (x, y, z) &\Leftrightarrow (\rho, \theta, \phi) & y = \rho \sin \theta \sin \phi & \theta = \cos^{-1} \frac{z}{\rho} \\
 && z = \rho \cos \theta & \phi = \operatorname{sgn}(y) \cos^{-1} \frac{z}{\sqrt{x^2 + y^2}}
 \end{aligned}$$

$$\begin{aligned}
 \hat{e}_\rho &= \sin \theta \cos \phi \hat{e}_x + \sin \theta \sin \phi \hat{e}_y + \cos \theta \hat{e}_z \\
 \hat{e}_\theta &= \cos \theta \cos \phi \hat{e}_x + \cos \theta \sin \phi \hat{e}_y - \sin \theta \hat{e}_z \\
 \hat{e}_\phi &= -\sin \phi \hat{e}_x + \cos \phi \hat{e}_y
 \end{aligned}$$

$$(r, \theta, z) \Leftrightarrow (\rho, \theta, \phi) \quad r = \rho \sin \phi \quad \rho = \sqrt{r^2 + z^2} \quad \theta = \tan^{-1} \frac{z}{r}$$

$$\text{Open cylinder: } dA_S = Rd\theta dz \rightarrow A_S = \int_0^{\ell} \int_0^{2\pi} R d\theta dz = 2\pi R\ell$$

$$\text{Sphere: } dA_S = R^2 \sin \theta d\theta d\phi \rightarrow A_S = \int_0^{2\pi} \int_0^\pi R^2 \sin \theta d\theta d\phi = 4\pi R^2$$

$$\begin{aligned}
 \vec{v} \cdot \vec{w} &= v_1 w_1 + v_2 w_2 + v_3 w_3 = |\vec{v}| |\vec{w}| \cos \theta \\
 \vec{v} \times \vec{w} &= (v_2 w_3 - v_3 w_2) \hat{i} - (v_1 w_3 - v_3 w_1) \hat{j} + (v_1 w_2 - v_2 w_1) \hat{k} \\
 |\vec{v} \times \vec{w}| &= |\vec{v}| |\vec{w}| |\sin \theta| \\
 \angle \vec{v} \vec{w} &= \cos^{-1} \left( \frac{\vec{v} \cdot \vec{w}}{|\vec{v}| |\vec{w}|} \right) \quad \hat{v} = \frac{\vec{v}}{|\vec{v}|} \quad \vec{v}_{(\parallel \hat{w})} = \vec{v} \cdot \frac{\vec{w}}{|\vec{w}|}
 \end{aligned}$$

## 2 Equations and Laws

Torricelli:  $\vec{v} = \sqrt{2gh}$

Newton's Law of Viscosity:  $\tau_{ij} = \mu \left( \frac{\partial \vec{v}_i}{\partial x_j} + \frac{\partial \vec{v}_j}{\partial x_i} \right)$

Fourier's Law of Heat Conduction:  $\Phi_Q = \frac{\dot{Q}_x}{A} = -k \nabla T$

Newtonian Constitutive:  $\boldsymbol{\tau} = \mu [\nabla \vec{v} + (\nabla \vec{v})^\top]$

Continuity:  $\frac{\partial \rho}{\partial t} + \vec{v} \cdot \nabla \rho = \rho (\nabla \cdot \vec{v})$   
(micro  $m$ )

Navier-Stokes:  $\rho \left( \frac{\partial \vec{v}}{\partial t} + \vec{v} \cdot \nabla \vec{v} \right) = -\nabla P + \mu \nabla^2 \vec{v} + \rho \vec{g}$

Gen. eqn. of motion:  $\rho \left( \frac{\partial \vec{v}}{\partial t} + \vec{v} \cdot \nabla \vec{v} \right) = -\nabla P + \nabla \cdot \boldsymbol{\tau} + \rho \vec{g}$   
(micro  $\bar{P}$ )

Energy:  $\rho \left( \frac{\partial \hat{E}}{\partial t} + \vec{v} \cdot \nabla \hat{E} \right) = -\nabla \cdot \Phi_Q - \nabla(P\vec{v}) + \nabla \cdot (\boldsymbol{\tau} \cdot \vec{v}) + \dot{Q}$   
(micro  $E$ )

Thermal energy:  $\rho \hat{C}_P \left( \frac{\partial T}{\partial t} + \vec{v} \cdot \nabla T \right) = k \nabla^2 T + \boldsymbol{\tau}^\top : \nabla \vec{v} + \dot{Q}$   
( $\Delta P, \Delta \rho = 0$ )

Hagen-Poiseuille:  $\dot{V} = \frac{\pi R^4 (\rho g \ell \cos \theta + \Delta P)}{8 \mu \ell}$

## 3 Fluid Mechanics

$$\dot{V} = A_\sigma \langle \vec{v} \rangle = \frac{\dot{m}}{\rho} \quad (\rho \vec{v}) = \frac{\dot{m}}{A_\sigma} \quad \rho_1 A_\sigma \langle \vec{v}_1 \rangle = \rho_2 A_\sigma \langle \vec{v}_2 \rangle$$

$$\frac{\Delta P}{\rho} + \frac{\Delta (\vec{v}^2)}{2\alpha} + g\Delta z + \sum \hat{F} = \frac{\dot{W}_{s,by}}{\dot{m}} \quad \alpha \approx 1, \text{ turbulent}$$

### 3.1 Force Losses

$$\text{Re} = \frac{\langle \vec{v} \rangle \rho \mathcal{D}}{\mu} \quad f = \frac{\mathcal{D}}{\ell} \frac{\Delta P}{2\rho \langle \vec{v} \rangle^2} = \frac{2\vec{F}_d}{\rho \langle \vec{v} \rangle^2 2\pi r \ell} \quad \text{Fr} = \frac{\langle \vec{v} \rangle^2}{g \mathcal{D}}$$

$$f_{\text{smooth, lam}} = 16/\text{Re} \quad f_{\text{smooth, trb}} = 0.079 \text{Re}^{-0.25}$$

$$\hat{F}_{\text{straight pipe}} = 4f \frac{\ell}{\mathcal{D}} \frac{\langle \vec{v} \rangle^2}{2} = \frac{\Delta P}{\rho} \quad \hat{F}_{\text{fitting}} = K_f \frac{\langle \vec{v} \rangle^2}{2}$$

$$\sum \hat{F} = \sum_i 4f_i \frac{\ell_i}{\mathcal{D}_i} \left( \frac{\langle \vec{v} \rangle_i^2}{2} \right) + \sum_j K_{f,j} \left( \frac{\langle \vec{v} \rangle_j^2}{2} \right)$$

$$\mathcal{D}_h = \frac{4A_\sigma}{\text{Perimeter}} \quad \tilde{H}_i = \frac{\hat{F}_i}{g} \quad \tilde{H} = \frac{\Delta P}{\rho g}$$

$$\vec{F}_d = \frac{1}{2} \rho \langle \vec{v} \rangle^2 A_\sigma C_d$$

$$\text{Drop: } C_d = \frac{2V_{\text{body}}(\rho_{\text{body}} - \rho)g}{\rho A_\sigma v_\infty^2} \quad \vec{v}_\infty = \sqrt{\frac{2V_{\text{body}}(\rho_{\text{body}} - \rho)g}{\rho A_\sigma C_d}}$$

### 3.2 Quantities of Interest

$$\hat{n} \equiv \langle n_1, n_2, n_3 \rangle \quad \boldsymbol{\sigma} = -P\mathbf{I} + \boldsymbol{\tau}$$

$$\dot{m} = (\vec{v} \cdot \hat{n}) A_\sigma \rho \quad \frac{d\vec{P}}{dt} = (\vec{v} \cdot \hat{n}) A_\sigma \rho \vec{v}$$

$$\dot{V} = \iint_S (\hat{n} \cdot \vec{v}) |_{\text{sfc}} dS \quad \langle \vec{v}_{\text{flow}} \rangle = \frac{\dot{V}}{\int_0^h \int_0^\ell dx dy}$$

$$\vec{F} = \iint_S [\hat{n} \cdot \boldsymbol{\sigma}] |_{\text{sfc}} dS \quad \vec{F}_z = \hat{e}_z \cdot \vec{F}$$

$$\vec{r} = \iint_S [\vec{r} \times (\hat{n} \cdot \boldsymbol{\sigma})] |_{\text{sfc}} dS$$

### 3.3 Macroscopic Balance

$$\frac{d\vec{P}}{dt} + \sum \left( \frac{1}{\beta} \rho A \cos \theta \langle \vec{v} \rangle^2 \hat{v} \right)_i = \sum (-PA\hat{n})_i + \vec{F}_{\text{on fluid}} + m_{\text{cv}} \vec{g}$$

$$\beta \approx 1, \text{ turbulent} \quad \beta = 0.75, \text{ laminar} \quad \cos \theta = \hat{n}_i \cdot \hat{v}_i \quad \hat{v}_i = \langle v_1, v_2, v_3 \rangle_i$$

## 4 Heat Transfer

$$\text{Conduction: } \frac{\dot{Q}_x}{A} = -k \frac{dT}{dx} = \frac{k(T_1 - T_2)}{\Delta x} \quad k [=] \frac{\text{W}}{\text{mK}}, \frac{\text{kg m}}{\text{s}^3 \text{K}}$$

$$\text{1-D: } T_{xyz} = -\frac{C_1}{k} x + C_2 \quad T_{r\theta z} = -\frac{C_1}{k} \ln r + C_2$$

$$\text{Generalised: } \dot{Q} = \frac{T_1 - T_N}{\sum R_i} \quad R_i \equiv \frac{\Delta x_i}{k_i A} = \frac{1}{h_i A} \quad U = \frac{1}{A \sum R_i}$$

$$\text{Convection: } |\frac{\dot{Q}_x}{A}| = h |(T_{\text{bulk}} - T_{\text{wall}})|$$

$$\begin{aligned}
 \text{Nu} &\equiv \frac{h\ell'}{k} \quad \text{Pr} \equiv \frac{C_P \mu}{k} \quad \text{Gr} \equiv \frac{\ell'^3 \rho^2 g \beta \Delta T}{\mu^2} \quad \ell' \in \{\varnothing, \delta, \ell\} \\
 \beta &\equiv T_{\text{film}}^{-1} \quad T_{\text{film}} = \frac{T_{\text{bulk}} + T_{\text{wall}}}{2}
 \end{aligned}$$

### 4.1 Heat Exchangers

$$\dot{Q} = UA \Delta T_{\text{lm}} f_T \quad \dot{Q}_{\text{water}} = \dot{m} \hat{C}_P \Delta T \quad \dot{Q}_{\text{steam}} = \dot{m} \Delta_{\text{vap}} \hat{H}$$

$$\Delta T_{\text{lm}} = \frac{(T_{\text{out, shell}} - T_{\text{in, tube}}) - (T_{\text{in, shell}} - T_{\text{out, tube}})}{\ln \frac{T_{\text{out, shell}}}{T_{\text{in, shell}}} \frac{T_{\text{in, tube}}}{T_{\text{out, tube}}}} = \frac{\Delta T_{\text{side A}} - \Delta T_{\text{side B}}}{\ln \frac{\Delta T_{\text{side A}}}{\Delta T_{\text{side B}}}}$$

$$U_I = \left( \frac{1}{h_i} + \frac{(R_O - R_I) A_I}{k_A A_{\text{lm}}} + \frac{A_I}{A_O h_O} \right)^{-1}$$

$$U_O = \left( \frac{A_O}{A_I h_i} + \frac{(R_O - R_I) A_O}{k_A A_{\text{lm}}} + \frac{1}{h_O} \right)^{-1}$$

$$A_{\text{lm}} = \frac{A_O - A_I}{\ln(A_O/A_I)} \quad A_i = 2\pi R_i \ell$$

$$\text{Fouling: } U_I = \left( \frac{1}{h_i} + \frac{1}{h_{d,I}} + \frac{(R_O - R_I) A_I}{k_A A_{\text{lm}}} + \frac{A_I}{A_O h_O} + \frac{A_I}{A_O h_{d,O}} \right)^{-1}$$

$$C_{\min} \equiv \min \{ (\dot{m} \hat{C}_P)_H, (\dot{m} \hat{C}_P)_C \} \quad C_{\max} \equiv \max \{ (\dot{m} \hat{C}_P)_H, (\dot{m} \hat{C}_P)_C \}$$

$$\epsilon_{\text{counter}} = \frac{1 - e^{\left[ \frac{-U_A}{C_{\min}} \left( 1 - \frac{C_{\min}}{C_{\max}} \right) \right]}}{1 - e^{\left[ \frac{-U_A}{C_{\max}} \left( 1 - \frac{C_{\min}}{C_{\max}} \right) \right]}} \quad \epsilon_{\text{co}} = \frac{1 - e^{\left[ \frac{-U_A}{C_{\max}} \left( 1 + \frac{C_{\min}}{C_{\max}} \right) \right]}}{1 + \frac{C_{\min}}{C_{\max}}}$$

$$\dot{Q} = \epsilon C_{\min} (T_{\text{H,shell}} - T_{\text{C,tube}})$$

### 4.2 Radiation

$$A_\Omega = \frac{\dot{Q}_{\text{absorbed}}}{\dot{Q}_{\text{incident}}} \quad \varepsilon_\Omega = \frac{\dot{Q}_{\text{emitted}}}{\dot{Q}_{\text{emitted, blackbody}}} \quad \text{Blackbody: } A_\Omega, \varepsilon_\Omega = 1$$

$$\frac{\dot{Q}_{\text{emitted}}}{A} = \varepsilon_\Omega \sigma T^4 \quad \dot{Q}_{\text{abs, net}} = A \varepsilon_\Omega |_{T_{\text{sfc}}} \sigma (T_{\text{sfc}}^4 - T_{\text{bulk}}^4)$$

$$\sigma \equiv 5.676 \text{E}-8 \frac{\text{J}}{\text{s m}^2 \text{K}^4}$$

$$h_{\text{rad}} = \frac{\varepsilon|_{T_{\text{sfc}}} \sigma (T_{\text{sfc}}^4 - T_{\text{bulk}}^4)}{T_{\text{sfc}} - T_{\text{bulk}}} \quad \dot{Q}_{\text{cnv+rad}} = (h_{\text{cnv}} + h_{\text{rad}}) A (T_{\text{sfc}} - T_{\text{bulk}})$$

$$\frac{\dot{Q}_{1 \rightarrow 2}}{A} = \frac{\sigma (T_1^4 - T_2^4)}{\varepsilon_1 + \frac{1}{\varepsilon_2} - 1} \quad N \text{ heat shields: } \frac{\dot{Q}_{1 \rightarrow 2}}{A} = \frac{1}{N+1} \frac{\sigma (T_1^4 - T_2^4)}{\sum \frac{1}{\varepsilon} - 1}$$

## 5 Fluid Mechanics Cases

Hydrostatic column:  $P_\perp = P_\perp + \rho gh$

U-manometer:  $P_A - P_B = (\rho_f - \rho_A) gh_f + (\rho_B - \rho_A) gh_B$

Sphere creep:  $\vec{F}_d = 6\pi R \mu \vec{v}_\infty \quad \vec{v}_\infty = \frac{4(\rho_{\text{body}} - \rho) \mathcal{D}^2 g}{18\mu} \quad \text{Re} = \frac{24}{C_d}$

Sphere drop:  $C_d = \frac{4(\rho_{\text{body}} - \rho) \mathcal{D} g}{3\rho v_\infty^2} \quad \vec{v}_\infty = \sqrt{\frac{4(\rho_{\text{body}} - \rho) \mathcal{D} g}{3\rho C_d}}$

### 5.1 Poiseuille Flow of Newtonian Fluid in Tube (Figure 1)

$$P(z) = \frac{P_\ell - P_0}{\ell} z + P_0 \quad \tau_{rz}(r) = \frac{P_\ell - P_0 - \rho g \ell}{2\ell} r$$

$$\vec{v}(r) = \langle 0, 0, \frac{(\rho g \ell + P_0 - P_\ell) R^2}{4\mu \ell} (1 - \left[ \frac{r}{R} \right]^2) \rangle$$

$$\langle \vec{v}_z \rangle = \frac{\int_0^{2\pi} \int_0^R \vec{v}_z r dr d\theta}{\int_0^{2\pi} \int_0^R r dr d\theta} \quad \vec{F}_{z,\text{wall}} = \int_0^\ell \int_0^{2\pi} \tau |_{r=R} R d\theta dz$$

$$\dot{V} = \int_0^{2\pi} \int_0^R \vec{v}_z r dr d\theta = \pi R^2 \langle \vec{v}_z \rangle$$

### 5.2 Newtonian Fluid Flow Down Inclined Plane (Figure 2)

$$g = \langle g \sin \theta, 0, g \cos \theta \rangle \quad \vec{v} = \langle 0, 0, \vec{v}_z \rangle$$

$$\vec{v}_z(x) = \frac{\rho g \cos \theta}{2\mu} (h^2 - x^2) \quad \langle \vec{v}_z \rangle = \frac{\int_0^w \int_0^h \vec{v}_z dx dy}{\int_0^w \int_0^h dx dy}$$

$$\dot{V} = \int_0^w \int_0^h \vec{v}_z dx dy = wh \langle \vec{v}_z \rangle \quad \vec{F}_{z,\text{wall}} = \int_0^\ell \int_0^w \tau_{xz} |_{x=h} dy dz$$

## 6 Heat Transfer Cases

Across rect. slab:  $T = \frac{T_2 - T_1}{\Delta x} x + T_1 \quad T_1 > T_2$

Across slab between bulk fluids, Newton's Law of Cooling B.C.:

$$\frac{\dot{Q}_x}{A} = \frac{T_{b1} - T_{b2}}{\frac{1}{h_1} + \frac{\Delta x}{k} + \frac{1}{h_2}} \quad T_{b1} > T_{b2}$$

$$T = T_{b1} - \frac{(T_{b1} - T_{b2}) \frac{1}{k}}{\frac{1}{h_1} + \frac{\Delta x}{k} + \frac{1}{h_2}} x + \frac{(T_{b1} - T_{b2}) \frac{1}{h_1}}{\frac{1}{h_1} + \frac{\Delta x}{k} + \frac{1}{h_2}}$$

$$\text{Cyl. shell: } \frac{\dot{Q}_r}{A} = \frac{T_1 - T_2}{\ln \frac{R_O}{R_I}} \frac{k}{r} \quad \frac{T_2 - T}{T_2 - T_1} = \frac{\ln \frac{R_O}{r}}{\ln \frac{R_O}{R_I}}$$

Annulus, Newton's Law of Cooling B.C. (Figure 3):

$$\frac{\dot{Q}_r}{A} = \frac{T_{b1} - T_{b2}}{\frac{1}{h_O R_O} + \frac{1}{k} \ln \frac{R_O}{R_I} + \frac{1}{h_I R_I}} \left( \frac{1}{r} \right) \quad T_{b1} > T_{b2}$$

$$T = T_{b2} + \frac{(T_{b1} - T_{b2})(\ln \frac{R_O}{r} + \frac{k}{h_O R_O})}{\frac{k}{h_O R_O} + \ln \frac{R_O}{R_I} + \frac{k}{h_I R_I}}$$

Wire with generation:  $\frac{T - T_s}{QR^2(4k)^{-1}} = 1 - \left( \frac{r}{R} \right)^2$

Very large  $h$ : use Fourier's Law

## 7 Heat Transfer Correlations

### 7.1 Forced Convection

$$\dot{Q} = \langle h \rangle A \Delta \langle T \rangle = \langle h \rangle A \frac{1}{2} [(T_{\text{wall}} - T_{\text{bulk,in}}) + (T_{\text{wall}} - T_{\text{bulk,out}})]$$

Lam.,  $\leftrightarrow$  pipe,  $\{\text{Re} < 2100, \text{RePr} \frac{\dot{Q}}{\ell} > 100\}$ :

$$\langle \text{Nu} \rangle = \frac{\langle h \rangle \phi}{k} = 1.86 \left( \text{RePr} \frac{\dot{Q}}{\ell} \right)^{1/3} \left( \frac{\mu_{\text{bulk}}}{\mu_{\text{wall}}} \right)^{0.14}$$

Trb., smooth pipe,  $\{\text{Re} > 6000, 0.7 < \text{Pr} < 16000, \ell/\phi > 60\}$ :

$$\text{Nu}_{\text{lm}} = \frac{h_{\text{lm}} \phi}{k} = 0.027 \text{Re}^{0.8} \text{Pr}^{1/3} \left( \frac{\mu_{\text{bulk}}}{\mu_{\text{wall}}} \right)^{0.14}$$

$$\text{Trb., air (1 atm), pipe: } h_{\text{lm}} = \frac{3.52 \bar{v}^{0.8}}{\phi^{0.2}}$$

$$\text{Trb., water, pipe, } \{4 \leq T \leq 105^\circ\text{C}\} : h_{\text{lm}} = 1429(1+0.0146T)^{\frac{\phi^{0.8}}{0.2}}$$

$$\text{Organic liquid: } h_{\text{lm}} = 423 \frac{\bar{v}^{0.8}}{\phi^{0.2}}$$

$$\text{Around sphere, } \{1 \leq \text{Re} \leq 7E4, 0.6 \leq \text{Pr} \leq 400\} : \text{Nu} = 2 + 0.6 \text{Re}^{\frac{1}{2}} \text{Pr}^{\frac{1}{3}}$$

### 7.2 Immersed Body

$$\text{Flow } \parallel \text{ plate, } \{\text{Re} < 3E5 \wedge \text{Pr} > 0.7\} : \text{Nu} = 0.664 \text{Re}^{0.5} \text{Pr}^{1/3}$$

$$\text{Flow } \parallel \text{ plate, } \{\text{Re} > 3E5 \wedge \text{Pr} > 0.7\} : \text{Nu} = 0.0366 \text{Re}^{0.8} \text{Pr}^{1/3}$$

$$\text{Flow } \perp \text{ cyl, } \{\text{Pr} > 0.6\} : \text{Nu} = C \text{Re}^m \text{Pr}^{1/3}$$

Re	$m$	$C$
1 – 4	0.330	0.989
4 – 40	0.385	0.911
$40 - 4 \times 10^3$	0.466	0.683
$4 \times 10^3 - 4 \times 10^4$	0.618	0.193
$4 \times 10^4 - 2.5 \times 10^5$	0.805	0.0266

### 7.3 Natural Convection

$$\downarrow \text{ plane/cyl: } \text{Nu} = \frac{h \ell}{k} = a(\text{GrPr})^m$$

Geometry	GrPr	$a$	$m$
$\downarrow \text{ plane/cyl, } \{h < 1 \text{ m}\}$	$< 10^4$	1.36	0.2
	$10^4 - 10^9$	0.59	0.25
	$> 10^9$	0.13	1/3
$\leftrightarrow \text{ cyl, } \{\phi < 0.2 \text{ m}\}$	$< 10^{-5}$	0.49	0
	$10^{-5} - 10^{-3}$	0.71	0.04
	$10^{-3} - 1$	1.09	0.1
	$1 - 10^4$	1.09	0.2
	$10^4 - 10^9$	0.53	0.25
	$> 10^9$	0.13	1/3
$\leftrightarrow \text{ plate, } \top \text{ heated / } \perp \text{ cooled}$	$10^5 - 2 \times 10^7$	0.54	0.25
	$2 \times 10^7 - 3 \times 10^{10}$	0.14	1/3
$\leftrightarrow \text{ plate, } \perp \text{ heated / } \top \text{ cooled}$	$10^5 - 10^{11}$	0.58	0.2

### 7.3.1 Simplified Natural Convection

Geometry	GrPr	$h (T[-]K, \ell[-]m)$
$\downarrow \text{ plane, cyl.}$	Air at 1 atm $10^4 - 10^9$ $> 10^9$	$1.37(\Delta T/\ell)^{0.25}$ $1.24(\Delta T)^{1/3}$
$\leftrightarrow \text{ cyl.}$	$10^3 - 10^9$ $> 10^9$	$1.32(\Delta T/\phi)^{0.25}$ $1.24(\Delta T)^{1/3}$
$\leftrightarrow \text{ plate, } \top \text{ heated / } \perp \text{ cooled}$	$10^5 - 2 \times 10^7$ $2 \times 10^7 - 3 \times 10^{10}$	$1.32(\Delta T/\ell)^{0.25}$ $1.52(\Delta T)^{1/3}$
$\leftrightarrow \text{ plate, } \perp \text{ heated / } \top \text{ cooled}$	$3 \times 10^5 - 10^{10}$	$0.59(\Delta T/\ell)^{0.25}$
$\downarrow \text{ plane, cyl.}$	Water at 294 K $10^4 - 10^9$	$127(\Delta T/\ell)^{0.25}$
$\downarrow \text{ plane, cyl.}$	Organic liquids at 294 K $10^4 - 10^9$	$59(\Delta T/\ell)^{0.25}$

### 7.3.2 Enclosed Spaces

Geometry	$\text{Gr}_{\delta} \text{Pr}$	$\text{Nu}_{\delta}$
$\downarrow \text{ plates, gas, } \{\ell/\delta < 3\}$	$< 2000$ $6 \times 10^3 - 2 \times 10^5$ $2 \times 10^5 - 2 \times 10^7$	1.0 $\frac{0.20(\text{Gr}_{\delta} \text{Pr})^{0.25}}{(\ell/\delta)^{1/9}}$ $\frac{0.073(\text{Gr}_{\delta} \text{Pr})^{1/3}}{(\ell/\delta)^{1/9}}$
$\downarrow \text{ plates, liquid}$	$< 1000$ $1000 - 10^7$	1.0 $\frac{0.28(\text{Gr}_{\delta} \text{Pr})^{0.25}}{(\ell/\delta)^{0.25}}$
$\leftrightarrow \text{ plates, gas, } \{T_{\perp} > T_{\top}\}$	$7 \times 10^3 - 3 \times 10^5$ $> 3 \times 10^5$	$0.21(\text{Gr}_{\delta} \text{Pr})^{0.25}$ $0.061(\text{Gr}_{\delta} \text{Pr})^{1/3}$
$\leftrightarrow \text{ plates, gas, } \{T_{\perp} > T_{\top}\}$	$1.5 \times 10^5 - 1 \times 10^9$	$0.069(\text{Gr}_{\delta} \text{Pr})^{1/3} \text{Pr}^{0.074}$

### 7.4 Boiling and Condensation

$$\text{Boiling, } \leftrightarrow, \{\frac{\dot{Q}}{A} < 16 \text{ kW m}^{-2}\} : h = 1043(\Delta T[\text{K}])^{1/3}$$

$$\text{Boiling, } \leftrightarrow, \{16 < \frac{\dot{Q}}{A} < 240 \text{ kW m}^{-2}\} : h = 5.56(\Delta T[\text{K}])^3$$

$$\text{Boiling, } \downarrow, \{\frac{\dot{Q}}{A} < 3 \text{ kW m}^{-2}\} : h = 537(\Delta T[\text{K}])^{1/7}$$

$$\text{Boiling, } \uparrow, \{3 < \frac{\dot{Q}}{A} < 63 \text{ kW m}^{-2}\} : h = 7.95(\Delta T[\text{K}])^3$$

$$\text{Boiling, forced convection: } h = 2.55(\Delta T[\text{K}])^3 e^{P[\text{kPa}]/1551}$$

$$\text{Boiling, film, } \leftrightarrow \text{ tube: } h = 0.62 \left[ \frac{k_{(\text{v})}^3 \rho_{(\text{v})} (\rho_{(\text{l})} - \rho_{(\text{v})}) g (\Delta_{\text{vap}} \hat{H} + 0.4 \hat{C}_{P_{(\text{v})}} \Delta T)}{\phi \mu_{(\text{v})} \Delta T} \right]$$

$$\text{Cond., film, bottom of } \downarrow \text{ sfc.: } \text{Re} = \frac{4 \pi \ell_{\perp}}{\ell' \mu_{(\text{l})}} \begin{cases} < 1800: \text{turbulent} \\ > 1800: \text{laminar} \end{cases} \quad \ell' = \frac{\pi \phi (\text{tube})}{\ell (\text{plate})}$$

$$\text{Cond., film, lam., } \downarrow \text{ tube: } \text{Nu} = 1.13 \left[ \frac{\rho_{(\text{l})} (\rho_{(\text{l})} - \rho_{(\text{v})}) g \Delta_{\text{vap}} \hat{H} (T_{\text{sat}}) \ell^3}{\mu_{(\text{l})} k_{(\text{l})} \Delta T} \right]^{0.25}$$

$$\text{Cond., film, trb., } \downarrow \text{ tube: } \text{Nu} = 0.0077 \left( \frac{\rho_{(\text{l})}^2 g \ell^3}{\mu_{(\text{l})}^2} \right)^{\frac{1}{3}} \text{Re}^{0.4}$$

$$\text{Cond., film, lam., outside } N \text{ stacked } \leftrightarrow \text{ cyl.: } \text{Nu} = 0.725 \left[ \frac{\rho_{(\text{l})} (\rho_{(\text{l})} - \rho_{(\text{v})}) g \Delta_{\text{vap}} \hat{H} \phi^3}{N \mu_{(\text{l})} k_{(\text{l})} \Delta T} \right]^{0.25}$$

## 8 Figures

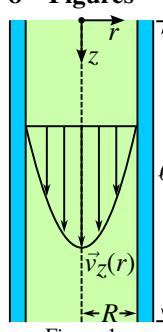


Figure 1

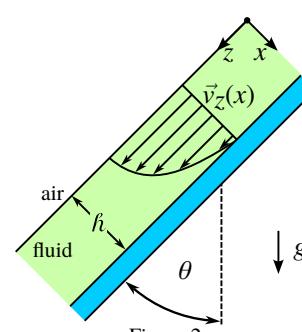


Figure 2

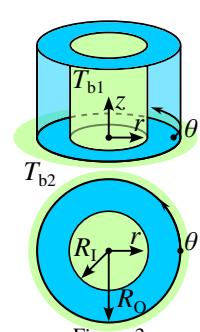


Figure 3

## References

ISBN-13: 9781107003538, 9780139304392